For B. on \mathbb{R}^d , let $T_R = Hifting time of $D_R(0)$$ In flee . 55.21 , we showed that

 $lim_{b\rightarrow\infty}uP$ $|B_t|$ = 00 $\forall\alpha\in(0,\frac{1}{2})$ P^o $h \rightarrow \infty$ \therefore $P(T_R < \infty) = \sqrt{R}$

Note : the P)
2 $-$ law of B , is equal to the \mathbb{P}^{ϵ} $-$ law of $x+B$. So we can always translate questions about balls $D_R(x)$ to $D_R(0)$.

we've seen that, on IR, we can exactly calculate the *(clistribution* of the) Hitting time of any height r >^o : ^t $P^{\circ}(\top_{r} \leq t) = P(1B_{t} | \geq r) = \sqrt{\frac{r}{2\pi u^{3}}}$

what about in higher dimensions ?

Pf. (of connection to the Divichlet problem)

Let reD. By definition

 $u(x) = \mathbb{E}^x[\int (B\tau_D) 1[\tau_D < \infty]$

If $x \in \partial D$, $\tau_D = O P^2 - a.s.$ and
 $\therefore uv \in F^2[f(B_0)] = f(x)$.

$u(x) = \mathbb{E}^{x}[F(B)] = \mathbb{E}^{x}[F(B_{s+})]$ where $F(w) = f(w(\tau_0)) \mathbb{1}_{\{\tau_0 < \omega\}}$

PDE tools can be used to stow that if
aD is sufficiently regular, u is in $C(D)$. Indeed, the easier statement of the Dirichlet problem $is: if \quad u,v \in C(D)$ and $\Delta u = \Delta v = o \text{ on } D$, then $u=v$.

The upshot is: if we can find a function ūs C(D)
s.t. $u = \bar{u} \mid_{D}$ is harmonic, then we must have

 $u(x) = E^{x}[\overline{u}(B\tau_{D}) 1\frac{1}{\pi} \sqrt{x} \sqrt{u}]$

 $5 = 0$ $D_R(x)$

For $d \ge 2$, define $u_d : \mathbb{R}^d \setminus \{0\} \to \mathbb{R}$ by

Rearranging this, we find:

