

Theorem: Let $(X_n)_{n\in\mathbb{N}}$ be a time-homogeneous Markov chain in (S, \mathcal{B}) with transition operator Q. Let $f: \mathbb{N} \times S \to \mathbb{R}$ be measurable, satisfying $E(If(n, X_n)] < \infty \quad \forall rv.$ Then Zn = f(n, Xn) is a martingale, provided $(Qf)(ntl, \cdot) = f(n, \cdot) \forall n \in \mathbb{N}$ (In particular, if $f: S \rightarrow \mathbb{R}$ doesn't depend on n, the condition is $\mathbb{R}f = f$ $Pf E[Z_{n+1}|F_n] = E[f(n+1, X_{n+1})|F_n] = Qf(n+1, X_n)$ One way to make this work, at least for a finite time interval OSAST, is to run the Markov chain backwards $f(n, y) := (Q^{-n}g)(y)$ for some $g: S \rightarrow IQ$. So (Zn=(Q^{T-n}g)(Xn))osnet is a martingale



	(2) (2)	
$M_n = f_n(n, X_n) =$	$(p\lambda + (1-p)\lambda')$ $\lambda^{(n)}$	is a martingall

