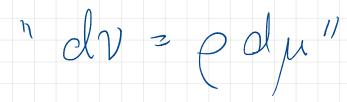
When is there a Density?

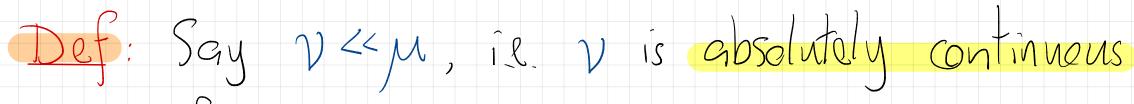
Let M, V be the measures on (RF).

How can we tell if I density pel(27)



There is one fairly straightforward necessary condition:

Suppose AEF and M(A)



S.t.

Theorem (Radon - Nikodym)

Let My be 5-finite measures on (27).

Then $v \ll \mu$ if and only if $\exists \rho: \Omega \rightarrow (0,\infty)$ measurable s.t.

 $v(A) = \int_A e^{-\beta A} e^{-\beta A} e^{-\beta A} = \int_A e^{-\beta A} e^{-\beta A} = \int_A e^{-\beta A} e^{-\beta A} e^{-\beta A} e^{-\beta A} = \int_A e^{-\beta A} e^{-\beta A} e^{-\beta A} e^{-\beta A} e^{-\beta A} = \int_A e^{-\beta A} e^{-\beta A} e^{-\beta A} e^{-\beta A} e^{-\beta A} = \int_A e^{-\beta A} e^{-\beta A} e^{-\beta A} e^{-\beta A} e^{-\beta A} e^{-\beta A} = \int_A e^{-\beta A} e^{-\beta$

I.e. $dv = \rho d\mu$

Moreover, this density p is uniquely defined up to a u-null set. It is called the Radon-Nikodyn derivative

 $e = \frac{dv}{d\mu}$

Theorem (Lebesque) [20.8]

- Let M, V be $\overline{\sigma}$ -finite measures on (Ω, \overline{f}) . Then V has a unique Lebesgue decomposition

 $\gamma = \gamma_a + \gamma_s$

where

