MATH 180A: INTRO TO PROBABILITY (FOR DATA SCIENCE)

www.math.ucsd.edu/~tkemp/180A



Screencast & video available after each lecture @ podcast.ucsd.edu

Before /After slides now available on course webpage.

Lots of active discussion on Piazza.

<u>Conditional Probability</u> Eg. Your friend rolls two fair dice, and asks you what is the probability the sum is 10.

Before you answer, however, she reveals that the actual sum that came up was a two digit number. In light of this information, was your probability calculation correct?

Conditional Probability

- Moral: given information (ie that an event B is known to have happened), we condition on B; we make B the new sample space.
 - We must modify events afterward so they're "in" B:

A B B





Suppose we somehow know a priori that at least one red is sampled. What is the conditional probability that exactly two red balls are sampled?

A = Eexactly 2 red} B= Eat least one red }

Recovering P from P(·1B)

By definition, $P(B|A) = \frac{P(AB)}{P(A)}$; \Rightarrow



Two-Stage Experiments

* perform an experiment, measure a random outcome. * perform a second experiment whose setup depends on the outcome of the first!





Subtler question: 90% of coins are fair, 9% are biased to come up heads 60% 1% are biased to come up heads 80%. You find a coiro on the street. You toss it, and it comes up heads. How likely is it that this Givo is heavily biased?

Eq. According to Forbes Magazine, as of April 10, 2019, there are 2208 billionaires in the Norld. 1964 of them are men.



Epidemeological Confusion

An HIV test is 99% accurate (1% false positives, 1% false negatives.) 0.33% of US residents have HIV.

If you test positive, what is the probability you have HIV?

(0) 99%

(b) 1 º/o

(C) 25%

(d) 0.33%

(e) There is not enough information to answer