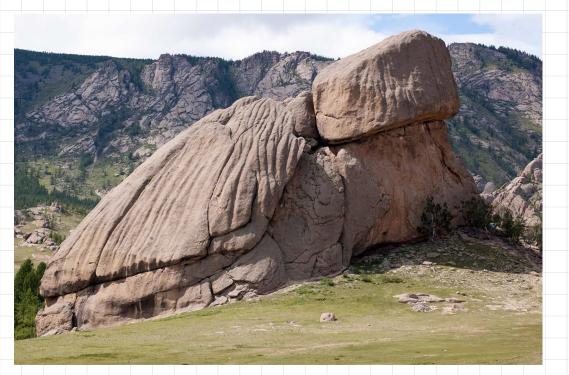
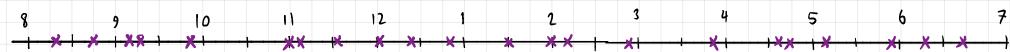
MATH 180A: INTRO TO PROBABILITY (FOR DATA SCIENCE)

www.math.ucsd.edu/~tkemp/180A

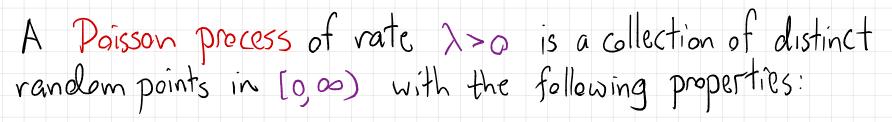


Lab4 due TONIGHT by 11:59pm HW4 due Friday (Nov8) by 11:59pm L> Error in problem statement of Exercise 4.40: the exact probability is = 0.00327556 # 0.000949681 Li-Tien the lemur hangs out at Turtle Rock all day. He observes that cars pass by rarely, randomly, on average every 30 minutes. He marks the times they come by on a number line:









(1) For any bounded interval (a,b] (05a<b<∞) the number

 $N((a,b]) := \#\{points in (a,b]\} \sim Poisson(\lambda(b-a))$

4.6

(2) For any non-overlapping intervals I₁= (a,b,1,..., I_k= (ak,bk), the random variables N(I,), N(I₂),..., N(I_k) are independent.

 $Useful notation: N_t = N((0,t]). Then N((a,b]) =$

(Nt) tra is an example of a stochastic process.

Special kind of stochastic process, with independent increments. (Sometimes called

a L'evy process.)

family of random variables indexed by time; usually with nice properties relating the distributions at different times. (MATH 180B/C)

Not easy to achieve.

Theorem: Let $X \sim Poisson(\lambda)$ and $Y \sim Poisson(\mu)$. If X, Y are independent, then

X+Y~~

Proof: Think about bionomials (of the same success rate).

Example: Customers arriving at the Art of Espresso in the afternoon arrive according to a Poisson process with rate 20/hour (a) What is the probability no one Gmes between 2pm and 2:15pm?

(b) What is the probability that 2 customers one between 2pm and 2:15pm, and 5 customers come between 2:15pm and 2:20pm?

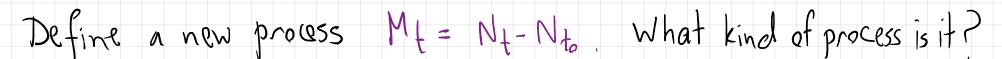
Let $(N_t)_{t=0}$ be a Poisson process of intensity $\lambda > 0$. Let T be the time of the first jump (i.e. first customer/car/etc.)

What is the distribution of T? I.e. find its CDF.

Constant Renewal

Let (Nt) tra be a Paisson process of intensity 2>0.

Fix some to ? 0.



Example: In a Poisson process of intensity λ , what is the distribution of the time interval between the 999th event and the loopth ?

