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1. Use unary predicates  $Dog(x)$  and  $Cat(x)$ , the binary predicate  $Likes(x, y)$ , the constant symbol  $Spot$ , the unary function  $Mother(x)$  and the equality sign  $=$  to express the following English sentences in first-order logic.  $Dog(x)$  means “ $x$  is a dog” and  $Cat(x)$  means “ $x$  is a cat”.  $Likes(x, y)$  means “ $x$  likes  $y$ ”.  $Mother(x)$  denotes the mother of  $x$ . Variables ranges over the universe of all dogs and cats.

- (a)  $Spot$  likes every cat.
- (b) All cats like  $Spot$ .
- (c) Some cat likes  $Spot$ .
- (d) At least two cats like  $Spot$ .
- (e) All dogs like each other.
- (f) No dog is the mother of a cat.
- (g) Each cat that likes themselves also likes  $Spot$ .
- (h) The mother of any cat is a cat.
- (i) Every cat and their mother like each other.
- (j)  $Spot$  is not a mother.