Math 160A - Fall 2021 - Quiz #6 - Upload by 9:30am, Wednesday, October 20.

Start Time: Your name:

Stop Time: Integrity signature:

Time limit 15 minutes, not counting download and upload. Please add explanation below if over 17 minutes total.

 $\frac{\text{PL axioms:}}{\text{PL1: } A \to B \to A}$ 

PL2:  $(A \to B \to C) \to (A \to B) \to (A \to C)$ 

PL3:  $\neg A \to A \to B$ PL4:  $(\neg A \to A) \to A$ 

•  $A \vee B$  and  $A \wedge B$  stand for  $\neg A \to B$  and  $\neg (A \to \neg B)$ .

**1.** Prove that there exists a PL-proof of  $A \to B \to A \wedge B$ .

**2.** Prove that there exists a PL-proof of  $\neg(A \land B) \rightarrow \neg A \lor \neg B$ .