## Math 155A - Fall 2021 - Quiz #1 - Hand in by 9:30am, October 1.

## Start Time:Your name:Stop Time:Integrity signature:

Time limit 15 minutes. Please add explanation below if over 17 minutes total.

- **1.** Use the variables
  - f "The coffee pot falls"
  - $\boldsymbol{b}$  "The coffee pot breaks"
  - g "The coffee pot is made of glass"
  - t "The coffee pot is made of titanium"

and propositional connectives  $\neg, \lor, \neg, \rightarrow, \leftrightarrow$  to express the sentences (a)-(g) as propositional formulas. When necessary, use parentheses to clarify the meaning of the propositional formulas. (You do not need include all the parentheses required in the formal definition of formulas.)

- (a) The coffee breaks only if it is made of glass.
- (b) The coffee breaks if it is made of glass and it falls.
- (c) The coffee pot is made of titanium or glass but not both.
- (d) The coffee pot falls if and only if it is made of glass.
- (e) The coffee pot falls but does not break.
- (f) The coffee does not break unless it is made of glass.
- (g) The coffee pot falls, but it does not break unless it is made of glass.

**2.** Using the same variables and **only** the connectives  $\land$  and  $\leftrightarrow$ , express the English sentence "The coffee pot is made of titanium or glass but not both" as a propositional formula. (It is possible you already gave this answer in part (c) above; if so, just reuse that answer.)