Student ID:

Name:

## CSE 167 - Intro to Computer Graphics - Fall 2004 Quiz #4 Answers — November 22 — Interpolation

**1.** Let  $\mathbf{x} = \langle -2, 1, 0 \rangle$  and  $\mathbf{y} = \langle 0, 1, -2 \rangle$ .

- **a.** What is  $Lerp(\mathbf{x}, \mathbf{y}, -1)$  equal to? Answer:  $\langle -4, 1, 2 \rangle$ .
- **b.** For what  $\alpha$  is  $Lerp(\mathbf{x}, \mathbf{y}, \alpha) = \langle -\frac{1}{2}, 1, -1\frac{1}{2} \rangle$ ? Answer:  $\alpha = \frac{3}{4}$ .

**2.** A triangle has vertices  $\mathbf{x}, \mathbf{y}, \mathbf{z}$  as shown. Also shown are seven points  $\mathbf{u}_1 - \mathbf{u}_7$ . For the following choices of barycentric coordinates indicate which point has those coordinates.

- **a.**  $\alpha = 1, \beta = 0, \gamma = 0.$ Answer: **x**.
- **b.**  $\alpha = \frac{1}{2}, \beta = 0, \gamma = \frac{1}{2}.$ Answer:  $\mathbf{u}_7$ .
- **b.**  $\alpha = \frac{1}{6}, \beta = \frac{2}{3}, \gamma = \frac{1}{6}.$ Answer:  $\mathbf{u}_3$ .

**3.** A quadrangle has vertex  $\mathbf{u}$ ,  $\mathbf{v}$ ,  $\mathbf{w}$ ,  $\mathbf{x}$  as shown. Give the formula for the point which is found using bilinear interpolation with  $\alpha = \frac{1}{2}$  and  $\beta = \frac{1}{3}$ . Your formula should not involve  $\alpha$  and  $\beta$ , instead use the particular values for  $\alpha$  and  $\beta$ . (Remark: Here the point  $\mathbf{u}$  is found  $\alpha = 0, \beta = 0$  and the point  $\mathbf{v}$  with  $\alpha = 1, \beta = 0$ .)



Answer:  $\frac{1}{3}\mathbf{u} + \frac{1}{3}\mathbf{v} + \frac{1}{6}\mathbf{x} + \frac{1}{6}\mathbf{y}$ .