

Errata Geometric Invariant Theory

over the real and complex numbers

- p. 63 line -8 replace is non-trivial with $\mathcal{O}(V)^G \neq \mathbb{C}1$.
- p. 88 line 9 replace \mathfrak{a} with V .
- p. 97 line 6 delete the $\frac{1}{2}$ in Lemma 3.79 2.
- p. 98 line 9 the right hand side of the equation should say

$$|W| \sum_{k=1}^n \left(\frac{1}{d_k} + \frac{d_k - 1}{2d_k} (1 - q) + o(1 - q) \right) \prod_{j \neq k} \frac{1 - q}{1 - q^{d_j}}$$

- p. 104-105 Replace Proposition 3.86 with
Lemma 3.86. (H, V) be a Vinberg pair with Cartan subspace \mathfrak{a} . Then

$$\dim H + \dim \mathfrak{a} \geq \dim V.$$

If the pair is regular then $\mathfrak{n} = 0$ and the inequality is equality.

Proof. We have seen that $H(\mathfrak{a} + \mathfrak{n})$ has non-empty Zariski interior in V . Also if

$$U = [C_G(\mathfrak{a}), C_G(\mathfrak{a})], \mathfrak{u} = \text{Lie}(U), M = \text{Ad}_{\mathfrak{u}}(U)_{|\mathfrak{u} \cap V}^\theta$$

then

$$(M, \mathfrak{u} \cap V)$$

is a Vinberg pair. We note that $\mathfrak{u} \cap V = \mathfrak{n}$. Thus every element is nilpotent. This implies that \mathfrak{n} consists of a finite number of nilpotent orbits. Hence one of them, Mx , must be open in \mathfrak{n} . This implies that

$$\dim V = \dim H - \dim C_G(\mathfrak{a})_x^\theta + \dim \mathfrak{a}.$$

If the pair is regular then have $C_G(\mathfrak{a})$ has a maximal torus in its centralizer. Since it is reductive and there can't be semi-simple elements in $\text{Lie}(C_G(\mathfrak{a}), C_G(\mathfrak{a}))$. We see that $\text{Lie}(C_G(\mathfrak{a}), C_G(\mathfrak{a})) = 0$. Thus $C_G(\mathfrak{a})^\theta = T_{\mathfrak{a}}$. Hence $\dim C_G(\mathfrak{a})^\theta = 0$.

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- p. 111 line 13 replace $e^{\frac{2\pi i}{3}ad_2}$ with $e^{\frac{2\pi i}{3}adH_2}$
at the end of theorem 3.100 the 8 should be replaced with 12.
- p. 117 line -3 the sum should be over k
line -1 delete the sum in the left side of the equation and the subscript of h in the determinant on the right hand side should be a j . That is the last line should read

$$\det \frac{\partial g_k}{\partial x_j} \det \frac{\partial h_j}{\partial t_k}(x_i, g_1, \dots, g_n) = (-1)^n \prod_{i=1}^n \frac{\partial h_i}{\partial t_0}(x_i, g_1, \dots, g_n).$$