

Winter 2024 Math 120A Homework 7

Due Mon. 11:59pm, March 4th PT.

Submit this homework through Gradescope. If you are not familiar with Gradescope, check the website for an instruction on how to use Gradescope.

Solve the following problems. Please show your work.

1. Let $z_0 = x_0 + iy_0$ with $x_0, y_0 \in \mathbb{R}$. Prove $(e^{z_0 t})' = z_0 e^{z_0 t}$. Here the derivative is taken with respect to t .
2. Compute $\int_0^1 (2 - it)^2 dt$.
3. Compute $\int_0^{\frac{\pi}{8}} e^{4it} dt$.
4. Compute $\int_C \frac{z-2}{z} dz$, where C is the contour $z = 2e^{it} : 0 \leq t \leq \pi$.

Academic Integrity for the homework: For the homework, you are allowed to discuss the homework problems with your classmates, Sharv and also me. But you need to write your solution down all by yourself. Simply copying the solution from other sources will be regarded as academic violation.

Note: Depending on the assigned workload for our grader, possibly only a subset of the questions will be graded for correctness. But you are supposed to finish all the above problems (the completeness of all problems also counts some points).