

1. (a) second order linear (b) first order linear (c) first order nonlinear
(d) second order nonlinear (e) first order linear
2. Compute $y_1'y_2 - y_1y_2'$ (the Wronskian) and see if it is nonzero at some point.
Alternatively verify that one function is not a constant multiple of the other.
3. There are 3: $y = -1$ is stable, $y = 0$ is unstable and $y = +1$ is stable.
Your answer should show how you got these results.
4. (a) The answer is $2 \sin(3t)$. The general solution is $c_1 \sin(3t) + c_2 \cos(3t)$. By the
initial conditions, $c_1 = 2$ and $c_2 = 0$.
Your solution should show how the general solution was found.
(b) Separate variables: $\int e^{-x} dx = \int e^t dt$ and so $-e^{-x} = e^t + C$. The initial condition
gives $-e^{-1} = 1 + C$ and so $C = -1 - e^{-1}$. Another way to write it:
 $e^{-x} + e^t = 1 + 1/e$.
(c) The equation is exact. Integrating gives $x^2 + xy - y^2 = C$.
(d) Divide by t to get it in standard form. An integrating factor is $\exp(\int -dt/t) = 1/t$.
Thus $y'/t - y/t^2 = 1$ and so $(y/t)' = 1$. Solving, $y/t = t + C$. You could rewrite
this as $y = t^2 + Ct$.