

NAME:

PID:

MATH 20C, SECTION A07

October 28, 2014

Quiz 2

Show all your work for full credit. To maximize credit, cross out incorrect work.

No credit will be given for unsupported answers.

1. (10 points) Find a normal vector to the plane through

$$P = (1, 0, 1), \quad Q = (1, 1, 0), \quad R = (0, 1, 1).$$

Solution

$$\vec{n} = \vec{PQ} \times \vec{PR}$$

$$\begin{aligned} \vec{PQ} &= \vec{OQ} - \vec{OP} = \langle 1, 1, 0 \rangle - \langle 1, 0, 1 \rangle \\ &= \langle 0, 1, -1 \rangle \end{aligned}$$

$$\begin{aligned} \vec{PR} &= \vec{OR} - \vec{OP} = \langle 0, 1, 1 \rangle - \langle 1, 0, 1 \rangle \\ &= \langle -1, 1, 0 \rangle \end{aligned}$$

$$\begin{aligned} \vec{PQ} \times \vec{PR} &= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 1 & -1 \\ -1 & 1 & 0 \end{vmatrix} \\ &= \hat{i}(0+1) - \hat{j}(0-1) + \hat{k}(0+1) \\ &= \hat{i} + \hat{j} + \hat{k} \quad (\text{or}) \quad \langle 1, 1, 1 \rangle \end{aligned}$$

Alternate solution:

$$\vec{n} = -\hat{i} - \hat{j} - \hat{k} \quad (\text{or}) \quad \langle -1, -1, -1 \rangle$$

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Good luck! ☺