MATH 100C Spring 2013

HOMEWORK 3

${\rm DUE}~24~{\rm APRIL}~2013$

- 1. (a) Find the lattice of the subfields F of $L = \mathbb{F}_{3^{16}}$ that contain $K = \mathbb{F}_{3^2}$.
 - (b) Determine which subfields F have the property that L/F is normal. Justify your answer.
 - (c) Determine which subfields F have the property that F/K is normal. Justify your answer.
- **2.** (a) Find the lattice of the subfields F of $K = \mathbb{Q}(\sqrt[3]{2}, \omega)$. Hint: they all contain \mathbb{Q} .
 - (b) Determine which subfields F have the property that K/F is normal. Justify your answer.
 - (c) Determine which subfields F have the property that F/\mathbb{Q} is normal. Justify your answer.
- **3.** Problems 1-7 from Section 8.3 in the textbook.