Math 20B



University of California, San Diego Department of Mathematics

Instructions

- 1. Write your Name, PID, Section, and the Version of your exam on the front of your Blue Book.
- 2. No calculators or other electronic devices are allowed during this exam.
- 3. You may use one page of notes, but no books or other assistance during this exam.
- 4. Read each question carefully, and answer each question completely.
- 5. Write your solutions clearly in your Blue Book
 - (a) Carefully indicate the number and letter of each question.
 - (\mathbf{b}) Present your answers in the same order they appear in the exam.
 - (c) Start each question on a new page.
- 6. Show all of your work; no credit will be given for unsupported answers.

1. (10 points) Find the area of the polar curve $r = \cos(3\theta)$ for $-\frac{\pi}{6} \le \theta \le \frac{\pi}{6}$.



2. (10 points) Evaluate the indefinite integral. You may leave your answer in exponential form.

$$\int \sin(3x)\cos(x)\,dx$$

3. (10 points) Evaluate the indefinite integral using the method of partial fractions.

$$\int \frac{x}{(x-1)^2(x^2+1)} \, dx$$

4. (10 points) Evaluate the indefinite integral.

$$\int \frac{1}{(9-x^2)^{3/2}} \, dx$$

5. (10 points) Evaluate the following improper integral:

$$\int_e^\infty \frac{1}{x(\ln x)^2} \, dx$$

(This exam is worth 50 points.)