## Math 20B



University of California, San Diego Department of Mathematics

Instructions

- 1. Write your Name, PID, and Section on the front of your Blue Book.
- 2. Write the Version of your exam on the front of your Blue Book.
- 3. No calculators or other electronic devices are allowed during this exam.
- 4. You may use one page of notes, but no books or other assistance during this exam.
- 5. Read each question carefully, and answer each question completely.
- 6. Write your solutions clearly in your Blue Book
  - (a) Carefully indicate the number and letter of each question.
  - (b) Present your answers in the same order they appear in the exam.
  - (c) Start each question on a new page.
- 7. Show all of your work; no credit will be given for unsupported answers.

1. (8 points) Find the area of the region enclosed by the curves  $y = x^2 + 3x - 2$  and y = 3x + 2.

- 2. Evaluate the following indefinite integrals:
  - (a) (8 points)  $\int \tan x \, dx$ (b) (10 points)  $\int \arctan x \, dx$
- 3. (8 points) Evaluate the definite integral:

$$\int_4^9 \frac{\sin\sqrt{x}}{\sqrt{x}} \, dx$$

4. (8 points) Let R be the region enclosed by the curves  $y = \sqrt{x^2 + 1}$  and  $y = e^{-x}$  between x = 0 and x = 1. (See figure below.) Compute the volume of the solid region obtained by rotating R about the x-axis.



5. (8 points) Find the volume of the solid with given base and cross sections: The base is the region enclosed by y = x and  $y = x^2$ . The cross sections perpendicular to the y-axis are semicircles.

(This exam is worth 50 points.)